חAMIBIA UCIVERSITY
OF SCIEПCE AПD TECHПOLOGY

## FACULTY OF HEALTH AND APPLIED SCIENCES

DEPARTMENT OF MATHEMATICS AND STATISTICS

| QUALIFICATION: Bachelor of science in Applied Mathematics and Statistics |  |
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| QUALIFICATION CODE: 08BHAM | LEVEL: 8 |
| COURSE CODE: ADC801S | COURSE NAME: ADVANCED CALCULUS |
| SESSION: JULY 2019 | PAPER: THEORY |
| DURATION: 3 HOURS | MARKS:100 |


| SUPPLEMENTARY/SECOND OPPORTUNITY EXAMINATION QUESTION PAPER |  |
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| EXAMINERS | DR ALFRED KAMUPINGENE |
| MODERATOR: | DR. D. MAKINDE |

THIS QUESTION PAPER CONSISTS OF 2 PAGES INCLUDING THIS COVER PAGE

| INSTRUCTIONS |
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| 1. Answer ALL the questions in the booklet provided. |
| 2. Show clearly all the steps used in the calculations. <br> 3. All written work must be done in blue or black ink and sketches must <br> be done in pencil. |
| 4. Start answering each of questions $1,2,3,4$, and 5 on a new page. |

## PERMISSIBLE MATERIALS

1. Non-programmable calculator without a cover.

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## Question 1 (16 marks)

Given the function $\mathrm{f}(\mathrm{x})=x^{n}$ where $x \varepsilon[\mathrm{a}, \mathrm{b}]$, prove that $\mathrm{n}(\mathrm{b}-\mathrm{a}) a^{n-1}<b^{n}-a^{n}<\mathrm{n}(\mathrm{b}-\mathrm{a}) b^{n-1}$ by applying the Langrage's Mean Value Theorem.

## Question 2(30 marks)

Factorise the following function $\mathrm{f}(\mathrm{x})=x^{4}-5 x^{3}+5 x^{2}+\mathrm{x}+2$ in terms of powers of $x-2$.

## Question 3(9 marks)

If $\varphi(x, y, z)=x y^{2} z$ and $\mathbf{A}=x z \mathbf{i}-x y^{2} \mathbf{j}+y z^{2} \mathbf{k}$, find $\frac{\partial^{3}(\varphi A)}{\partial z \partial x^{2}}$ at the point $(2,-1,1)$.

## Question 4(32 marks)

Consider the vector field $\mathbf{F}=\left(3 x^{2} y^{2} z+5 y^{3}, 2 x^{3} y z+15 x y^{2}-7 z, x^{3} y^{2}-7 y+4 z^{3}\right)$ with domain $R^{3}$.
4.1) Determine whether the above field is conservative.
4.2) If the field is, indeed, conservative, find a potential function for it.

## Question 5(13 marks)

Suppose a firm has an order for 200 units of its product and wishes to distribute their manufacture between two of its plants, plant1 and plant2. Let $q_{1}$ and $q_{2}$ denote the outputs of plants 1 and 2 , respectively, and suppose the total cost function is given by $C=f\left(q_{1}, q_{2}\right)=2 q_{1}{ }^{2}+q_{1} q_{2}+q_{2}{ }^{2}+200$. How should the output be distributed in order to minimise costs?

